

EASTERN UNIVERSITY SRI LANKA
 FACULTY OF COMMERCE AND MANAGEMENT
 FIRST YEAR, SECOND SEMESTER EXAMINATION IN
 BUSINESS ADMINISTRATION/ COMMERCE 2011/2012
 (AUGUST 2014) – PROPER / REPEAT / RE-REPEAT
 COM 1032 BASIC CALCULUS



Answer All Questions

Time: 02 Hours

01. (i) Find the domain of the following functions:

a) $f(x) = \frac{x^2 + 5}{x + 2}$ b) $f(x) = \sqrt{x^2 + 9}$

(04 marks)

(ii) a) If $f(x) = \begin{cases} -2x + 4 & \text{if } x \leq 1 \\ x^2 + 1 & \text{if } x > 1 \end{cases}$ then find

i) $f(3) + f(-5)$ ii) $f\left(\frac{f(0)}{f(2)}\right)$

(04 marks)

b) If $f(x) = x + 1$, and $g(x) = (x - 1)^3 + 2x^2$, then find $g(f(x))$.

(02 marks)

(iv) Evaluate the following limits:

a) $\lim_{x \rightarrow 1} \left(\frac{1}{x^2} - \frac{1}{x} \right)$

b) $\lim_{x \rightarrow 0} \frac{\sqrt{2+x} - \sqrt{2}}{x}$

c) $\lim_{x \rightarrow \alpha} \left(\frac{x^2 - 6x + 13}{2x^3 + 7x^2 - 11} \right)$

d) $\lim_{x \rightarrow 8} \left(x^{2/3} + 4x^{-1/3} - 5 \right)$

e) $\lim_{x \rightarrow 2} \left(\frac{x^3 - 8}{2 - x} \right)$

(15 marks)

[Total 25 Marks]

02. (i) Differentiate the following functions with respect to x :

a) $y = \sqrt{x}(\sqrt{x} + 3)$

b) $y = \frac{3x+2}{(x+2)(x^2-3)+3}$

c) $y = (x^2 + 2)e^{2x} \ln(x^2 + 2)$

d) $y = \left(\frac{2x^3+1}{3x^2+1}\right)^2$

(15 marks)

(ii) a) If $y = \frac{x}{1+x}$ then show that $x \frac{dy}{dx} = y(1-y)$.

(03marks)

b) If $x = t \ln t$ and $y = \frac{\ln t}{t}$, then find $\frac{dy}{dx}$ and evaluate it at $t=1$.

(04 marks)

c) If $e^{xy} - 4xy = 4$ then find $\frac{dy}{dx}$ in terms of x and y .

(03 marks)

d) If $y = e^{(-2x)} \ln 2x$, then find $\frac{d^3 y}{dx^3}$.

(03 marks)

[Total 28 Marks]

03. (i) Find the points of maxima and minima for the function,

$$y = x^4 - 8x^3 + 80x^2 + 15.$$

(07 Marks)

(ii) If the average cost function of a particular product is given by $AC = \frac{160}{x} + 5 - 3x + 2x^2$; where x is the number of units produced and sold.

Find the total cost function of the product.

(03 Marks)

(ii) A manufacturer has found that if he wants to increase his output, he must lower his price. His total revenue $R(x)$ from an output level x is given by the expression $R(x) = x(148 - x)$. His production costs are: Rs. 1000 as fixed cost and Rs. 36 per unit as variable cost. You are required to find the following:

- the output level that would maximize revenue;
- the maximum total revenue;
- the profit function $P(x)$;
- the output level that maximizes profit;
- the maximum total profit.

(15 Marks)

[Total 25 Marks]

04. (i) Integrate the following:

a) $\int \frac{x^3 + 5x^2 + 6x}{x^2} dx$

b) $\int x^{-2} \ln x dx$

c) $\int (2x^3 + 3x - 7)x^2 dx$

d) $\int x(2 + x^2)^{3/2} dx$

e) $\int \frac{2xe^{2x}}{e(2x+3)} dx$

(14 marks)

(ii) Evaluate the following:

a) $\int \frac{6x}{0x^2 + 1} dx$

b) $\int_{-1}^2 (4x^3 + 6x)^2 dx$

(05 marks)

(iii) The marginal cost function of a firm is given by $5000e^{0.5x} + 30$, where x the quantity is produced. If the fixed cost is Rs. 70000, find the total cost function of the firm.

(03 marks)

[Total 22 Marks]