

EASTERN UNIVERSITY, SRI LANKA

FIRST EXAMINATION IN SCIENCE – 2013/2014

SECOND SEMESTER (April/May 2016)

PH 103 ELECTRICITY AND MAGNETISM I



Time: 01 hour

Answer ALL Questions

Q1. State Gauss's law in electrostatics.

Figure 1 shows a spherical capacitor of charge  $Q$ , which is formed with two concentric conducting shells of inner radius  $a$  and outer radius  $b$ . The regions within the spherical shells from  $a$  to  $r$  and  $r$  to  $b$  are filled with the dielectric constants  $K_1$  and  $K_2$  respectively. The electric potentials at inner shell and the outer shell are  $V_a$  and  $V_b$  respectively.

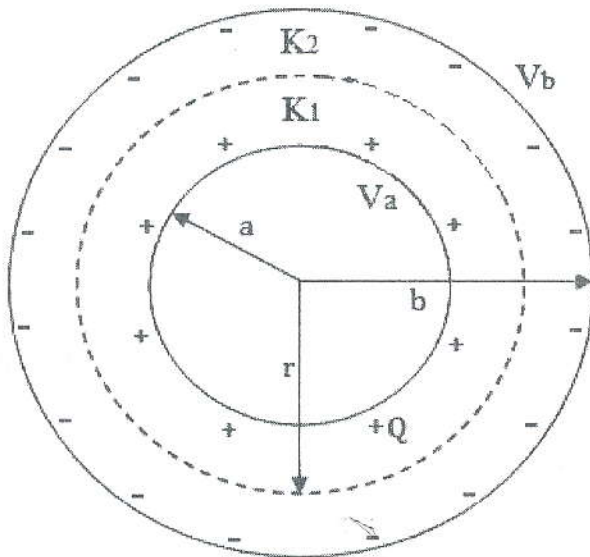


Figure 1

- Using Gauss's law, find an expression for electric field within the capacitor.
- Find the potential difference between the inner and the outer surfaces of the spherical shells.
- Determine the capacitance of the capacitor.

d) If  $K_1 = K_2 = 10$ ,  $a = 2$  cm,  $b = 5$  cm, and  $r = 3.5$  cm, then show that the capacitance of the capacitor is  $\frac{4}{3}\pi\epsilon_0$ .

e) If charge  $Q = 20$   $\mu\text{F}$ , then show that the energy stored in the capacitor is  $\frac{1}{2}QV$ .

Given that  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{Nm}^2\text{C}^{-2}$ , where  $\epsilon_0$  is the permittivity of free space.

02. State Biot-Savart law and hence derive an expression for the magnetic field formed by an infinitely long current carrying wire at a distance  $r$ .

Consider two long straight parallel current conductors A and B carrying currents  $I_1$  and  $I_2$  in opposite directions as shown in figure.

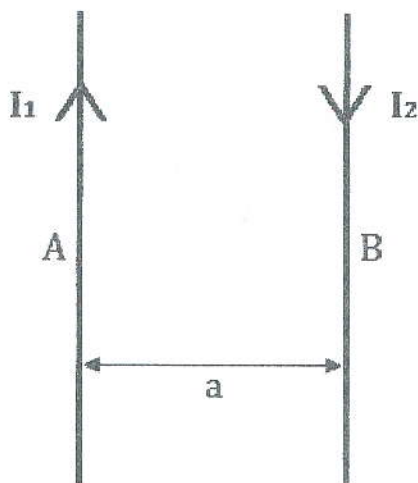


Figure 2

a) Determine the magnitude and the direction of the magnetic field formed by conductor A at conductor B.

b) Determine the magnitude and the direction of the force per unit length on conductor B.

c) Show that the magnitude of force per unit length on conductors A and B is the same.

d) If  $I_1 = 10$  A,  $I_2 = 8$  A, and  $a = 4$  cm, then calculate the force per unit length on the conductors.

e) If  $I_2$  is increased to 10A then find the increment in force per unit length on conductor B.

f) Illustrate the directions of forces on A and B, if the currents  $I_1$  and  $I_2$  are in the same direction.

Assume that the permeability of free space is  $\mu_0 = 4\pi \times 10^{-7} \text{Hm}^{-1}$ .