

EASTERN UNIVERSITY, SRI LANKA

SECOND EXAMINATION IN SCIENCE - 2009/2010

SECOND SEMESTER (PROPER/REPEAT)

(April 2012)

PH 103 - ELECTRICITY AND MAGNETISM



Time: 01 hour.

Answer ALL Questions

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1. State Gauss's theorem in electrostatics.

a) A conducting spherical volume of radius  $a$  carries a total positive charge  $Q$  distributed uniformly throughout it. Using Gauss's theorem, derive an expression for the electric field strength inside the sphere at a distance  $r$  from its center. Hence show that the electric potential inside the sphere at a distance  $r$  from the center is given by:

$$\frac{Q(3a^2 - r^2)}{8\pi\epsilon_0 a^3}$$

b) Using Gauss's theorem, derive an expression for the capacitance per unit length between two long coaxial cylindrical conductors of radius  $a$  and  $b$  ( $> a$ ) in air.

2. State Ampere's circuital law clearly identifying the quantities involved.

- a) As illustrated in figure (a), a coaxial line carries the same current  $I$  upward the inner conductor of radius  $a$ , and downward the outer conductor of inner radius  $b$  and outer radius  $c$ .

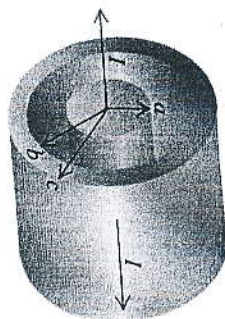


Figure (a)

Using Ampere's circuital law, find an expression for the magnitude of the magnetic field at a distance  $r$  from the conductor, when

- i.  $r < a$
  - ii.  $a < r < b$  and
  - iii.  $b < r < c$ .
- b) An infinitely long, cylindrical conductor of radius  $R$  carries a current  $I$  in the upward direction. The axis of the cylinder lies in a plane of a rectangular loop of wire with dimensions  $2R$  and  $L$ , as shown in the figure (b). The current  $I$  in the cylinder is uniformly distributed over its cross section perpendicular to its axis.

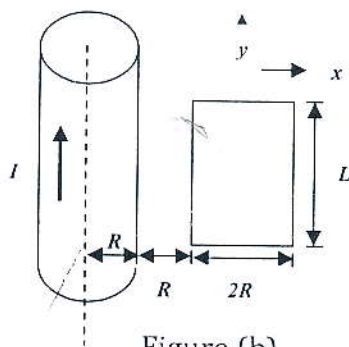


Figure (b)

- i. Using Ampere's circuital law, find an expression for the magnitude of the magnetic field at a distance  $r < R$ , measured from the axis of the cylinder.
- ii. Find the magnetic flux through the loop due to the current  $I$  in the cylinder.