

EASTERN UNIVERSITY, SRI LANKA

SECOND EXAMINATION IN SCIENCE – 2012/2013

SECOND SEMESTER (PROPER / REPEAT)

OCTOBER 2016

PH 206 WAVES AND VIBRATION



: 01 hour

er ALL Questions

- a. Define “spring constant” of a spring.(10 Points)
- b. An object of mass m is placed on a frictionless plane and connected with the end of a spring with spring constant k . The other end of the spring is fixed firmly on a wall.
- i. Show that the motion of the object is simple harmonic.(10 Points)
- ii. Show that the displacement of the object at any time t is given by:
 $x = A\sin(\omega_0 t + \phi)$, where the symbols have their usual meaning.
.....(10 Points)
- iii. Show that the maximum kinetic energy and potential energy of the object in the above case is: $\frac{1}{2}kA^2$(20 Points)
- iv. Hence show that the total energy of the system is constant.(10 Points)
- v. Sketch the variations of the potential energy and the kinetic energy of the object against the displacement in a single graph.(30 Points)

vi. A mass $m = 100$ g is attached at the end of a light spring with a spring constant $k = 250$ N/m. The other end of the spring is fixed firmly. The mass is pushed against the spring and compresses the spring from its relaxed position. The system is then released and the mass moves towards the opposite direction. If the friction is ignored, what distance will the mass be moved as it shoots away?

2.

a. What do you understand by the terms “relaxation time” and “quality factor” of a lightly damped harmonic oscillator?

b. The differential equation that describes a damped oscillator can be written as $m\ddot{x} + D\dot{x} + kx = 0$, where the symbols have their usual meanings.

i. Define the following terms using the parameters in the above equation, and describe the motion in each case: heavy damping, critical damping, and light damping.

ii. Obtain equations for the displacement x in the heavy damping and light damping cases.

iii. Show that the quality factor (Q) for the damped oscillator is

$$\frac{1}{D} \sqrt{km}$$

iv. Illustrate the relaxation time of the light damping is $\frac{m}{D}$.