04

Eastern University, Sri Lanka
Faculty of Commerce and Management
Special Repeat Examination in BBA/ COM- (2003/2004)
February/ March (2010)
DAF 3134 Business Statistics

Answer all questions

Time: 03 Hours.

- 01 a. (i) What are the conditions that must be satisfied by the probabilities in a discrete probability distribution?
- (ii) The number of defective parts produced per day by an automated machine follows a Poisson probability distribution with a mean of 4.
- a. What is the probability that on a given day at least two defective parts are produced?
- b. What is the probability that on 2 consecutive days exactly 4 defective parts are produced?
- c. What is the mean and standard deviation of the number of defective parts produced by the machine per day?
- b (i) What is meant by the standard normal distribution?
- (ii) The daily sales in a hardware store have a normal distribution with a mean of Rs. 2000 and a standard deviation of Rs. 165. Determine the probability that:
- a. Sales are between Rs. 1800 and Rs 2600
- b. sales are less than Rs.1500
- c. Sales exceeds Rs. 2500

(20 marks)

02. a. (i) State the central limit theorem.
- (ii) An auditor for a large credit card company knows that on average the monthly balance of any given customer is Rs. 11200 and the standard deviation is Rs. 5600. Fifty accounts are randomly audited and the sample mean of monthly balance, \bar{x} is calculated.
- a. What is the name of the sampling distribution of \bar{x} ?
- b. What are the mean and standard error of the sampling distribution of \bar{x} ?
- c. Find the probability that the sample mean of monthly balance is below Rs. 10000.

- b. (i) Explain the difference between a point estimate and an interval estimate.
- (ii) Several companies have been developing electronic guidance systems for cars. A and B are two firms in the forefront of such research. Out of 120 trials of A's model 101 were successful and out of 200 trials of B's model 110 were successful.
- compute the unbiased point estimate of the difference in two population proportions of developing successful electronic guidance system.
 - Construct 95% confidence interval for the difference in two population proportions of developing successful electronic guidance system.

(20 marks)

03. a. Explain the following terms

- Null hypothesis
- Alternative hypothesis
- Significant level

- b. A firm producing light bulbs wants to test if it can claim that the light bulbs it produces last 1000 burning hours. The firm takes a random sample of 100 of its light bulbs and finds that the sample mean is 1980 hours and the sample standard deviation is 80 hours. Test the claim at the 5% level of significance.

(20 marks)

04. The following data relate to training and performance of salesmen employed in a company.

Salesman	1	2	3	4	5
hours of training	20	05	10	13	12
Performance (Average weekly sales in 1000 Rs)	44	22	25	32	27

- Identify the independent variable and the dependent variable
- Compute the least squares regression line
- Estimate the weekly sales that are likely to be attained by a salesman who is given 16 hours of training
- Compute the correlation coefficient and coefficient of determination
- Interpret the results in the context of the data calculated in part (iv)

(20 marks)

05. a. The revenues (in Rs. millions) of a chain of Ice cream stores are listed for each quarter during the previous 5 years.

Quarter	2005	2006	2007	2008	2009
1	68	65	68	70	60
2	62	58	63	59	55
3	61	56	63	56	31
4	63	61	67	62	58

- (i) Calculate the four- quarter centered moving average
 - (ii) Using the moving averages computed in part (i) calculate the seasonal indexes
 - (iii) Interpret the seasonal indexes
- b. The following trend line and seasonal indexes were computed from 10 years of quarterly observations. Forecast the next year's time series.

$$\hat{y} = 150 + 3t \quad t = 1, 2, \dots, 40$$

Quarter	1	2	3	4
Seasonal index	0.7	1.2	1.5	0.6

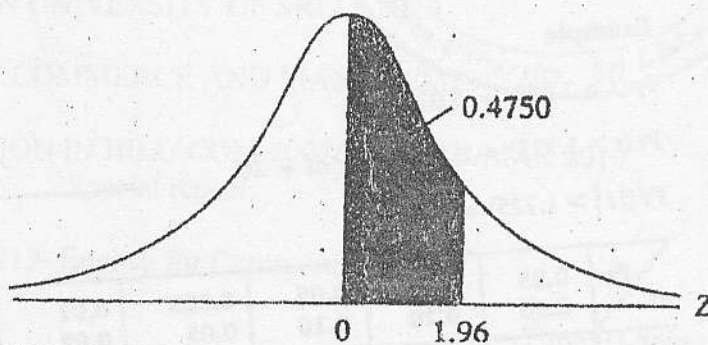
(20 marks)

Areas under the standardized normal distribution

Example

$$\Pr(0 \leq Z \leq 1.96) = 0.4750$$

$$\Pr(Z \geq 1.96) = 0.5 - 0.4750 = 0.025$$



Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4454	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990

Note: This table gives the area in the right-hand tail of the distribution (i.e., $Z \geq 0$). But since the normal distribution is symmetrical about $Z = 0$, the area in the left-hand tail is the same as the area in the corresponding right-hand tail. For example, $P(-1.96 \leq Z \leq 0) = 0.4750$. Therefore, $P(-1.96 \leq Z \leq 1.96) = 2(0.4750) = 0.95$.

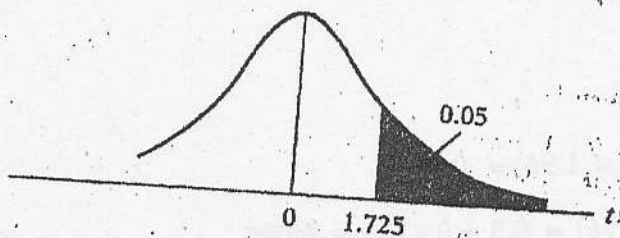
Percentage points of the t distribution

Example

$$\Pr(t > 2.086) = 0.025$$

$$\Pr(t > 1.725) = 0.05 \quad \text{for } df = 20$$

$$\Pr(|t| > 1.725) = 0.10$$



df \ Pr	0.25 0.50	0.10 0.20	0.05 0.10	0.025 0.05	0.01 0.02	0.005 0.010	0.001 0.002
1	1.000	3.078	6.314	12.706	31.821	63.657	318.31
2	0.816	1.886	2.920	4.303	6.965	9.925	22.327
3	0.765	1.638	2.353	3.182	4.541	5.841	10.214
4	0.741	1.533	2.132	2.776	3.747	4.604	7.173
5	0.727	1.476	2.015	2.571	3.365	4.032	5.893
6	0.718	1.440	1.943	2.447	3.143	3.707	5.208
7	0.711	1.415	1.895	2.365	2.998	3.499	4.785
8	0.706	1.397	1.860	2.306	2.896	3.355	4.501
9	0.703	1.383	1.833	2.262	2.821	3.250	4.297
10	0.700	1.372	1.812	2.228	2.764	3.169	4.144
11	0.697	1.363	1.796	2.201	2.718	3.106	4.025
12	0.695	1.356	1.782	2.179	2.681	3.055	3.930
13	0.694	1.350	1.771	2.160	2.650	3.012	3.852
14	0.692	1.345	1.761	2.145	2.624	2.977	3.787
15	0.691	1.341	1.753	2.131	2.602	2.947	3.733
16	0.690	1.337	1.746	2.120	2.583	2.921	3.686
17	0.689	1.333	1.740	2.110	2.567	2.898	3.646
18	0.688	1.330	1.734	2.101	2.552	2.878	3.610
19	0.688	1.328	1.729	2.093	2.539	2.861	3.579
20	0.687	1.325	1.725	2.086	2.528	2.845	3.552
21	0.686	1.323	1.721	2.080	2.518	2.831	3.527
22	0.686	1.321	1.717	2.074	2.508	2.819	3.505
23	0.685	1.319	1.714	2.069	2.500	2.807	3.485
24	0.685	1.318	1.711	2.064	2.492	2.797	3.467
25	0.684	1.316	1.708	2.060	2.485	2.787	3.450
26	0.684	1.315	1.706	2.056	2.479	2.779	3.435
27	0.684	1.314	1.703	2.052	2.473	2.771	3.421
28	0.683	1.313	1.701	2.048	2.467	2.763	3.408
29	0.683	1.311	1.699	2.045	2.462	2.756	3.396
30	0.683	1.310	1.697	2.042	2.457	2.750	3.385
40	0.681	1.303	1.684	2.021	2.423	2.704	3.307
60	0.679	1.296	1.671	2.000	2.390	2.660	3.232
120	0.677	1.289	1.658	1.980	2.358	2.617	3.160
∞	0.674	1.282	1.645	1.960	2.326	2.576	3.090

Note: The smaller probability shown at the head of each column is the area in one tail; the larger probability is the area in both tails.

Source: From E. S. Pearson and H. O. Hartley, eds., *Biometrika Tables for Statisticians*, vol. 1, 3d ed., table 12, Cambridge University Press, New York, 1966. Reproduced by permission of the editors and trustees of *Biometrika*.